

1. (currently amended) A method for multiplying an elliptic curve point $Q(x,y)$ by a scalar to provide a point kQ , the method comprising the steps of:

a) selecting an elliptic curve of order n over a finite field F such that there exists an endomorphism ψ where $\psi(Q) = \lambda(Q)$ for all point $Q(x,y)$ on the elliptic curve, and λ is an integer,

b) establishing a representation of said scalar k as a combination of components k_i and said

integer λ of the form $k_i = \sum_{i=0}^{i=n} k_i \lambda^i \text{ mod } n$.

c) combining said representation and said point Q to form a composite representation of a multiple of the form $k_0Q + k_1 \psi(Q) + \dots$ corresponding to kQ ; and

d) computing a value corresponding to said point kQ from said composite representation of kQ .

2. (original) A method according to claim 1 wherein each of said components k_i is shorter than said scalar k .

3. (original) A method according to claim 1 wherein said components k_i are initially selected and subsequently combined to provide said scalar k .

4. (currently amended) A method according to claim 1 wherein said components k_i are selected at random. [representation is of the form $k_i = \sum_{i=0}^{i=n} k_i \lambda^i \text{ mod } n$ where n is the number of points on the elliptic curve].

5. (currently amended) A method according to claim 4 wherein said representation is of the form $k_0 + k_1 \lambda$.

6. (currently amended) A method according to claim 1 wherein said scalar k has a predetermined value and said components k_0 and k_1 are one half size of said scalar k .

7. (original) A method according to claim 3 wherein said value of said multiple kQ is calculated using simultaneous multiple addition.
8. (original) A method according to claim 7 wherein grouped terms G_i utilized in said simultaneous multiple addition are precomputed.
9. (original) A method according to claim 6 wherein said components k_i are obtained by obtaining short basis vectors (u_0, u_i) of the field F , designating a vector v as $(k, 0)$, converting v from a standard, orthonormal basis to the (u_0, u_i) basis, to obtain fractions f_i representative of the vector v , applying said fractions to k to obtain a vector z , calculating an efficient equivalent v' in the composite representation of kQ .
10. (currently amended) A method of generating in an elliptic curve cryptosystem a key pair having a integer k providing a private key and a public key kQ , where Q is a point on the curve,
 - a) selecting an elliptic curve over a finite field F such that there exists an endomorphism ψ where $\psi(Q) = \lambda Q$ for all points $Q(x, y)$ on the elliptic curve, λ is an integer,
 - b) establishing a representation of said key k as a combination of components k_i and said integer λ , of the form $k_i = \sum_{i=0}^{i=n} k_i \lambda^i \text{ mod } n$ where n is the number of points on the elliptic curve,
 - c) combining said representation and said point Q to form a composite representation of a multiple of the form $k_0Q + k_1 \psi(Q) + \dots$ corresponding to the public key kQ ; and
 - d) computing a value corresponding to said public kQ from said composite representation of kQ .
11. (currently amended) A method according to claim 10 [including a method according to any one of claims 2 to 9] wherein each of said components k_i is shorter than said scalar k .
12. (new) A method according to claim 11 wherein said components k_i are initially selected and subsequently combined to provide said scalar k .
13. (new) A method according to claim 12 said components k_i are selected at random.

14. (new) A method according to claim 13 wherein said representation is of the form $k_0 + k_1 \lambda$.
15. (new) A method according to claim 10 wherein said scalar k has a predetermined value and said components k_0 and k_1 are selected to be one half the size of said scalar k .
16. (new) A method according to claim 12 wherein said value of said multiple kQ is calculated using simultaneous multiple addition.
17. (new) A method according to claim 16 wherein grouped terms G_i utilized in said simultaneous multiple addition are precomputed.
18. (new) A method according to claim 15 wherein said components k_i are obtained by obtaining short basis vectors (u_0, u_i) of the field F , designating a vector v as $(k, 0)$, converting v from a standard, orthonormal basis to the (u_0, u_i) basis, to obtain fractions f_i representative of the vector v , applying said fractions to k to obtain a vector z , calculating an efficient equivalent v' in the composite representation of kQ .